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`Dsuite` - Fast *D*-statistics and related admixture evidence from VCF files

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Abstract

Patterson's *D*, also known as the ABBA-BABA statistic, and related statistics such as the f_4-ratio, are commonly used to assess evidence of gene flow between populations or closely related species. Currently available implementations often require custom file formats, implement only small subsets of the available statistics, and are impractical to evaluate all gene flow hypotheses across data sets with many populations or species due to computational inefficiencies. Here, we present a new software package `Dsuite`, an efficient implementation allowing genome scale calculations of the *D* and f_4-ratio statistics across all combinations of tens or hundreds of populations or species directly from a variant call format (VCF) file. Our program also implements statistics suited for application to genomic windows, providing evidence of whether introgression is confined to specific loci, and it can also aid in interpretation of a system of f_4-ratio results with the use of the "*f*-branch" method. `Dsuite` is available at https://github.com/millanek/Dsuite, is straightforward to use, substantially more computationally efficient than comparable programs, and provides a convenient suite of tools and statistics, including some not previously available in any software package. Thus, `Dsuite` facilitates the assessment of evidence for gene flow, especially across larger genomic data sets.

KEYWORDS

ABBA-BABA, *D* statistic, f4-ratio, gene flow, introgression, software

1 | INTRODUCTION

Admixture between populations and hybridisation between species are common and a bifurcating tree is often insufficient to capture their evolutionary history (Green et al., 2010; Kozak et al., 2018; Malinsky et al., 2018; Patterson et al., 2012; Tung & Barreiro, 2017). Patterson's *D* statistic, first used to detect introgression between modern human and Neanderthal populations (Durand et al., 2011; Green et al., 2010), has been widely applied across a broad range of taxa (Fontaine et al., 2015; Kozak et al., 2018; Malinsky et al., 2018; Tung & Barreiro, 2017; vonHoldt et al., 2016). The *D* statistic and the related estimate of admixture fraction *f*, referred to as the f_4-ratio (Patterson et al., 2012), are simple to calculate and well suited

for taking advantage of genomic-scale data sets, while being robust under most demographic scenarios (Durand et al., 2011).

The *D* and f_4-ratio statistics belong to a class of methods based on studying correlations of allele frequencies across populations and were developed within a population genetic framework (Patterson et al., 2012). However, the methods can be successfully applied for learning about hybridisation and introgression within groups of closely related species, as long as common population genetic assumptions hold – namely that (a) the species share a substantial amount of genetic variation due to common ancestry and incomplete lineage sorting; (b) recurrent and back mutations at the same sites are negligible; and (c) substitution rates are uniform across species (Patterson et al., 2012; Pease & Hahn, 2015).

While the results of other methods such as PCA (Patterson et al., 2006), STRUCTURE (Pritchard et al., 2000), and ADMIXTURE (Alexander et al., 2009) may be hard to interpret historically, because they do not explicitly fit a historical model or unrealistically assume that all populations have radiated from a single ancestral group, the use of the D and f_4-ratio statistics involves fitting a simple explicit phylogenetic tree model to a quartet of populations or species (Figure 1a, b) and provides a formal test for a history of admixture in that context (Patterson et al., 2012). The treemix method (Pickrell & Pritchard, 2012), on the other hand, can fit a complex historical graph model of a tree with migration edges for a data set of many populations, but does not provide a rigorous test for whether any proposed migration edges are correct (Patterson et al., 2012; Pickrell & Pritchard, 2012). Finally, methods based on detailed population genetic models, such as δaδi (Gutenkunst et al., 2009), fastsimcoal2 (Excoffier et al., 2013), or IMa2 (Hey, 2010) can be used to infer demographic history that includes events such as population size changes, population splits and joins, and migration. However, these methods require data from multiple individuals per population or species, and, despite recent improvements in efficiency (Kamm et al., 2019), are computationally very demanding, limiting their application to a small number (generally < 10) of populations or species.

With more genomic data becoming available, there is a need for handling data sets with tens or hundreds of taxa. Applying the D and f_4-ratio statistics has the advantage of computational efficiency and is powerful even when using whole genome data from only a single individual per population (Green et al., 2010). On the other hand, as each calculation of D and f applies to four populations or taxa, the number of calculations/quartets grows rapidly with the size of the data set. The number of quartets is $\binom{n}{4}$, i.e. n choose 4, where n is the number of populations. This can present challenges in terms of increased computational requirements. Moreover, the resulting test statistics are correlated when quartets share an (internal) branch in the overall population or species tree, which may make a system of all possible four taxon tests across a data set difficult to interpret.

Because pinpointing specific introgression events in data sets with tens or hundreds of populations or species remains challenging, the f-branch or $f_b(C)$ metric was introduced in Malinsky et al. (2018) to disentangle correlated f_4-ratio results and assign gene flow evidence to specific, possibly internal, branches on a phylogeny. The f-branch metric builds upon and formalises verbal arguments employed by Martin et al. (2013) to assign gene flow to specific internal
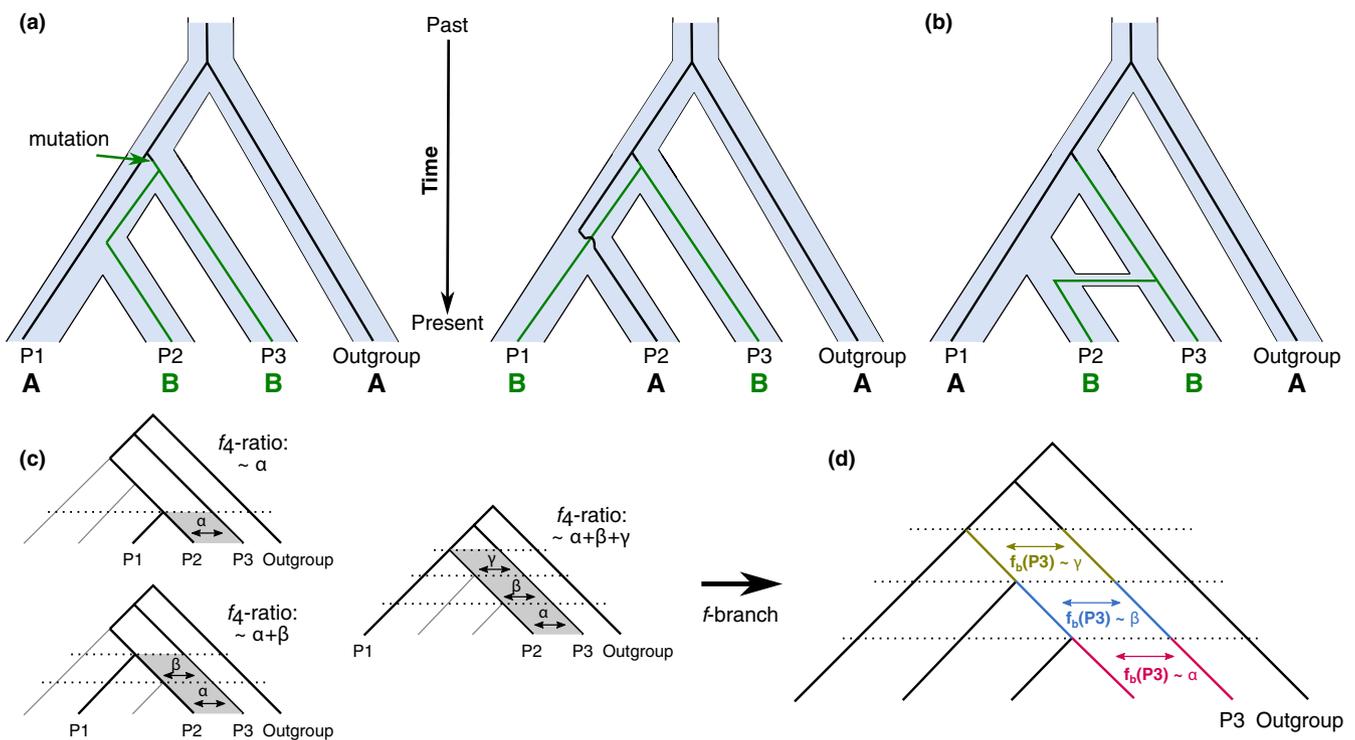

FIGURE 1 Basic principles behind the D and f-branch statistics. (a) Example genealogies showing the sharing of derived alleles, denoted as 'B' between populations P2 and P3 (the ABBA pattern) and between P1 and P3 (the BABA pattern) as a result of incomplete lineage sorting. In a scenario without gene flow, both patterns are assumed to be equally likely (but see (Eriksson & Manica, 2012 for exceptions). (b) Gene flow between P2 and P3 introduces additional loci with ABBA patterns, which would lead to a positive D statistic. (c) An example illustrating interdependences between different f_4-ratio scores, which can be informative about the timing of introgression. In this example, different choices for the P1 population provide constraints on when the gene flow could have happened. (d) Based on relationships between the f_4-ratio results from different four taxon tests, the f-branch, or f_b statistic, distinguishes between admixture at different time periods, assigning signals to different (possibly internal) branches in the population/species tree [Colour figure can be viewed at wileyonlinelibrary.com]

branches on the phylogeny of *Heliconius* butterflies. Thus, the *f*-branch statistic can be seen as an aid for formulating gene flow hypotheses in data sets of many populations or species.

Patterson's *D* and related statistics have also been used to identify introgressed loci by sliding window scans along the genome (Fontaine et al., 2015; Heliconius Genome Consortium, 2012), or by calculating these statistics for particular short genomic regions. Because the *D* statistic itself has large variance when applied to small genomic windows and because it is a poor estimator of the amount of introgression (Martin et al., 2015), additional statistics which are related to the *f*$_4$-ratio have been designed specifically to investigate signatures of introgression in genomic windows along chromosomes. These statistics include *f*$_d$ (Martin et al., 2015), its extension *f*$_{dM}$ (Malinsky et al., 2015), and the distance fraction *df* (Pfeifer & Kapan, 2019).

Programs for calculating Patterson's *D* and related statistics include ADMIXTOOLS (Patterson et al., 2012), HYDE (Blischak et al., 2018), ANGSD (Paul et al., 2011; Soraggi et al., 2018), POPGENOME (Pfeifer & Kapan, 2019; Pfeifer et al., 2014), and COMP-D (Mussmann et al., 2020). However, a number of factors call for an introduction of new software. First, most of the existing programs cannot handle the variant call format (VCF) (Danecek et al., 2011), the standard file format for storing genetic polymorphism data produced by variant callers such as SAMTOOLS (Li, 2011) and GATK (DePristo et al., 2011). Second, the computational requirements of these programs in terms of either run time or memory (or both) make comprehensive analyses of data sets with tens or hundreds of populations or species either difficult or infeasible. Third, the programs implement only a subset of the statistics discussed above, and there are some statistics, namely *f*$_{dM}$, and *f*-branch, which have not yet been implemented in any publicly available software package.

To address these issues, we introduce the Dsuite software package. Dsuite brings the calculation of different related statistics together into one software package, combining genome-wide and sliding window analyses, and downstream analyses aiding their interpretation (Table 1). Dsuite has a user-friendly straightforward workflow and uses the standard VCF format, thus generally avoiding the need for format conversions or data duplication. Moreover, Dsuite is computationally more efficient than other software in the core task in calculating the *D* statistics, making it more practical for analysing large genome-wide data sets with tens or even hundreds of populations or species. Finally, Dsuite implements the calculation of the *f*$_{dM}$ and *f*-branch statistics for the first time in publicly available software. While researchers can implement these and other statistics in their own custom scripts, the inclusion of the whole package of statistics in Dsuite facilitates their use and reproducibility of results.

2 | MATERIALS AND METHODS

2.1 | The *D* and *f*$_4$-ratio statistics

The *D* and *f*$_4$-ratio statistics can be presented as applying to biallelic SNPs across four populations or taxa: P1, P2, P3, and O, related by the rooted tree (((P1,P2),P3),O), where the outgroup O carries the ancestral allele, denoted by A, and the derived allele is denoted by B (Durand et al., 2011; Green et al., 2010; Pease & Hahn, 2015). The site patterns are ordered such that the pattern BBAA refers to P1 and P2 sharing the derived allele, ABBA to P2 and P3 sharing the derived allele, and BABA to P1 and P3 sharing the derived allele. Under the null hypothesis, which assumes no gene flow, the ABBA and BABA patterns are expected to occur due to incomplete lineage sorting with equal frequencies, and a significant deviation from that expectation is consistent with introgression between P3 and either P1 or P2. See Figure 1, (Patterson et al., 2012) and (Durand et al., 2011) for more detail.

While simple site pattern counts can be computed for single sequences, most implementations, including Dsuite, work with allele frequency estimates, so that multiple individuals can be included from each population or taxon. Denoting the derived allele frequency estimate at site *i* in P1 as $\hat{p}_{i1}$, and similarly $\hat{p}_{i2}$ and $\hat{p}_{i3}$ for populations P2 and P3, the following sums are calculated across all *n* biallelic sites:

$$nABBA = \sum_{i=1}^{n} (1-\hat{p}_{i1})\hat{p}_{i2}\hat{p}_{i3} \tag{1a}$$

$$nBABA = \sum_{i=1}^{n} \hat{p}_{i1}(1-\hat{p}_{i2})\hat{p}_{i3} \tag{1b}$$

$$nBBAA = \sum_{i=1}^{n} \hat{p}_{i1}\hat{p}_{i2}(1-\hat{p}_{i3}) \tag{1c}$$

where we assume that the outgroup is fixed for the ancestral allele (i.e., $\hat{p}_{iO}=0$). The *D* statistic is then simply a normalised difference between the ABBA and BABA patterns:

$$D = \frac{nABBA - nBABA}{nABBA + nBABA} \tag{2}$$

If the frequency of the derived allele in the outgroup is not zero, the results of Dsuite correspond to the *D* and *f*$_4$-ratio statistics as defined by Patterson et al. (2012), who present the statistics as applying to an unrooted four taxon tree, with O being simply a fourth population rather than an outgroup. Their *D* definition is:

$$D = \frac{\sum_{i=1}^{n} (\hat{p}_{i2}-\hat{p}_{i1}) * (\hat{p}_{i3}-\hat{p}_{iO})}{\sum_{i=0}^{n} (\hat{p}_{i2}+\hat{p}_{i1}-2*\hat{p}_{i2}*\hat{p}_{i1}) * (\hat{p}_{i3}+\hat{p}_{iO}-2*\hat{p}_{i3}*\hat{p}_{iO})} \tag{3}$$

In this case, the ancestral versus derived allele assignment is not necessary and the A and B labels can be assigned arbitrarily; the BAAB site pattern is equivalent to ABBA, ABAB to BABA, and AABB to BBAA. Therefore, the Patterson et al. (2012) definition of *D* corresponds to changing the right-hand side of Equation (1a–c) to:

$$nABBA = \sum_{i=1}^{n} (1-\hat{p}_{i1})\hat{p}_{i2}\hat{p}_{i3}(1-\hat{p}_{iO}) + \hat{p}_{i1}(1-\hat{p}_{i2})(1-\hat{p}_{i3})\hat{p}_{iO} \tag{4a}$$

TABLE 1 Statistics calculated by `Dsuite` and overlap with other software packages

Software	VCF input	Genome-wide tests/statistics			Sliding window statistics			
		D	f_4-ratio	f-branch	D	f_d	f_{dM}	df
ADMIXTOOLS		✓	✓					
ANGSD		✓						
COMP-D		✓						
HYDE		✓						
POPGENOME	✓	✓			✓	✓		✓
DSUITE	✓	✓	✓	✓	✓	✓	✓	✓

$$nBABA = \sum_{i=1}^{n} \hat{p}_{i1}\left(1-\hat{p}_{i2}\right)\hat{p}_{i3}\left(1-\hat{p}_{iO}\right) + (1-\hat{p}_{i1})\hat{p}_{i2}\left(1-\hat{p}_{i3}\right)\hat{p}_{iO} \quad (4b)$$

$$nBBAA = \sum_{i=1}^{n} \hat{p}_{i1}\hat{p}_{i2}(1-\hat{p}_{i3})\left(1-\hat{p}_{iO}\right) + (1-\hat{p}_{i1})\left(1-\hat{p}_{i2}\right)\hat{p}_{i3}\hat{p}_{iO} \quad (4c)$$

We note that this definition is different from the one used by Durand et al. (2011) and Martin et al. (2015), which implicitly assumes that the outgroup is fixed for the ancestral allele and should only be used in such cases. While with the above formulas (Equations 3 and 4a–c) it is technically not necessary for O to represent an outgroup, the current implementation of `Dsuite` makes this assumption in order to streamline the analysis and downstream interpretation of the results.

Calculating the f_4-ratio requires that P3 be split into two subsets, P3a and P3b, which is done in `Dsuite` by randomly sampling alleles from P3 at each SNP but is possible even if the data set contains only one diploid individual from P3, in which case the two alleles are both sampled from that one individual. The results in `Dsuite` then correspond to the Patterson et al. (2012) definition:

$$f_4 ratio = \frac{\sum_{i=1}^{n}\left(\hat{p}_{i3a}-\hat{p}_{iO}\right)*\left(\hat{p}_{i2}-\hat{p}_{i1}\right)}{\sum_{i=1}^{n}\left(\hat{p}_{i3a}-\hat{p}_{iO}\right)*\left(\hat{p}_{i3b}-\hat{p}_{i1}\right)} \quad (5)$$

2.2 | The *f*-branch statistic

The number of possible gene flow donor-recipient combinations increases rapidly with the number of populations or species. A unified test for introgression has been developed for a five taxon symmetric phylogeny, implemented in the D_{FOIL} package (Pease & Hahn, 2015). However, no such framework currently exists for data sets with six or more taxa. A common approach is to perform the D and f_4-ratio analyses on all four taxon subsamples from the data set (Green et al., 2010; Kozak et al., 2018; Malinsky et al., 2018; Martin et al., 2013; vonHoldt et al., 2016). However, the number of analyses that need to be performed grows very quickly. Even with a fixed outgroup, the number of combinations is $\binom{n}{3}$, i.e., *n* choose 3, where *n* is the number of taxa. For example, there are 1,140 different combinations of ((P1, P2), P3) in a data

set of 20 taxa, growing to 161,700 combinations in a data set with 100 taxa. Interpreting the results of such a system of four taxon tests is not straightforward; the different subsets are not independent as soon as the taxa share drift (that is, they share branches on the phylogeny) and, therefore, a single gene flow event can be responsible for many elevated D and f_4-ratio results. At the same time, the correlations, especially of the f_4-ratio scores, can be informative about the timing of introgression events and about the specific donor-recipient combinations.

The *f*-branch or f_b metric was introduced in Malinsky et al. (2018) to disentangle correlated f_4-ratio results and assign gene flow evidence to specific, possibly internal, branches on a phylogeny by building upon the logic developed by Martin et al. (2013), as illustrated in Figure 1. Given a specific tree (with known or hypothesised relationships), the f_b(P3) statistic reflects excess sharing of alleles between the population or species P3 and the descendants of the branch labelled b, relative to allele sharing between P3 and the descendants of the sister branch of b.

Formally:

$$f_b(P3) = median_A\left[min_B\left[f_4 ratio(A,B;P3,O)\right]\right] \quad (6)$$

where B refers to the populations or taxa descending from the branch b, and A refers to descendants from the sister branch of b. The calculation is over all positive f_4-ratio results which had A in the P1 and B in the P2 positions.

2.3 | Sliding window statistics

A number of statistics have been developed specifically for application to genomic windows. They can be used to assess whether the admixture signal is confined to specific loci and to assist in locating any such loci. The D statistic itself has large variance when applied to small genomic windows and it is a poor estimator of the amount of introgression (Martin et al., 2015). However, statistics related to the f_4-ratio have been found to perform better. The `Dsuite` package implements three of these statistics (Table 1). The first is f_d (Martin et al., 2015), which is defined as:

$$f_d = \frac{S(P1,P2,P3,O)}{S(P1,Pd,Pd,O)} \quad (7)$$

where $S(P1, P2, P3, O)$ stands for the numerator of D (i.e. $nABBA - nBABA$) and $S(P1, Pd, Pd, O)$ denotes the equivalent calculation but with $Pd = P2$ or $Pd = P3$, depending on which of these two populations has the higher frequency of the derived allele. While the f_d statistic may be useful to localise genomic regions introgressed between P2 and P3, it is not meaningful in cases of excess sharing of alleles between P1 and P3 and can take arbitrarily large negative values in those cases ($f_d < -1$). To address this issue, Malinsky et al. (2015) developed a modified version of the f_d statistic which: (i) under the null hypothesis of no introgression is symmetrically distributed around zero; and (ii) can equally quantify shared variation between P3 and P2 (positive values) or between P3 and P1 (negative values). They called this modified f_d statistic f_{dM}. The calculation of f_{dM} further depends on the frequency of the derived allele in P1 and P2. If the frequency of the derived allele in P2 is higher or equal to P1 then $f_{dM} = f_d$. However, if the derived allele frequency is higher in P1, then:

$$f_{dM} = \frac{S(P1, P2, P3, O)}{-S(Pd, P2, Pd, O)} \tag{8}$$

The final sliding window statistic implemented in `Dsuite` is the distance fraction df of Pfeifer & Kapan (2019), which is derived by combining the approach of studying correlation of allele frequencies (as in the other statistics presented here) with the concept of genetic distance. Specifically, $d_f = \frac{\sum_{i=1}^{n} \hat{p}_{i2} * \hat{d}_{i13} - \hat{p}_{i1} * \hat{d}_{i23}}{\sum_{i=1}^{n} \hat{p}_{i2} * \hat{d}_{i13} + \hat{p}_{i1} * \hat{d}_{i23}}$

where $\hat{d}_{xy}$ is an estimate of the genetic distance at variable sites between populations x and y, so $\hat{d}_{i13}$ is the distance between P1 and P3 at site i. This can be formulated as a function of allele frequencies:

$$d_{i13} = \hat{p}_{i1} + \hat{p}_{i3} - (2 * \hat{p}_{i1} * \hat{p}_{i3}) \tag{10}$$

and equivalently for P2 and P3. The distance fraction d_f shares the advantages of f_{dM} of being symmetric and bounded on the interval [−1,1], while it may provide a more accurate estimate of the amount of introgression, being less sensitive to the timing of gene flow (Pfeifer & Kapan, 2019). However, a thorough comparison of the advantages and disadvantages of all three sliding window statistics across a broad range of historical scenarios is lacking – therefore, it may be beneficial to consider the evidence provided by the combination of all three statistics.

2.4 | Implementation

The statistics described above are implemented in a set of programs and utilities within the `Dsuite` package. The first program, `Dtrios`, calculates the sums in Equation (4a–c) and outputs genome-wide statistics including the D, its associated p-value, and the f_4-ratio statistic, for all trios of populations or species. This enables the assessment of evidence for gene-flow across the entire data set. Next, `Dinvestigate` calculates the sliding window statistics (f_d, f_{dM}, and

df) for particular trios specified by the user. These programs take as input a VCF file (Danecek et al., 2011), whereby allele frequencies for each biallelic SNP and each population are calculated by default from the called genotypes (the GT field). In addition, we provide an option to use genotype probabilities (GP field) produced for example by phasing and imputation software such as BEAGLE (Browning & Browning, 2007), or genotype likelihoods (either GL or PL fields) produced by variant callers such as GATK (DePristo et al., 2011). More details are provided in Appendix S1. Using genotype likelihoods or probabilities instead of relying solely on called genotypes can be especially useful for low coverage data and can be taken advantage of by choosing the `-g` option to `Dtrios` and `Dinvestigate`. Missing genotypes (./.) or likelihoods/probabilities are handled as follows. When data are missing in a subset of samples from a population or species, the allele frequency is estimated from the remaining samples; if genotypes are missing in all individuals from the population or species then the site is ignored for all trios which contain that population or species. Although primarily designed for whole genome analyses, being based on allele frequencies, the programs are in principle also applicable to restriction-site-associated DNA sequencing (RADseq) data (Andrews et al., 2016) and other multilocus genomic data in VCF format. Results from `Dtrios` can be further processed using the `Fbranch` program and associated plotting utilities for the f-branch statistic, facilitating interpretation of the results. Finally, the utilities `DtriosCombine` and `DtriosParallel` enable analyses of large data sets by parallelisation of the workflow across compute nodes or across CPU cores on a single computer.

2.4.1 | The Dtrios program

`Dtrios` does not require a priori knowledge of population or species relationships, only the outgroup has to be specified. Instead, the command produces three types of output. For the first, in a file with the "BBAA.txt" suffix, `Dtrios` attempts to infer the population or species relationships: it orders each trio assuming that the correct tree is the one where the BBAA pattern is more common than the discordant ABBA and BABA patterns, which are assumed to result from incomplete lineage sorting or from introgression. The second type of output is the D_{min} score, the minimum D for each trio regardless of any assumptions about the tree topology. There is no attempt to infer the true tree; instead, the trio is ordered so that the difference between $nABBA$ and $nBABA$ is minimized. This output is in a file with the "Dmin.txt" suffix and can be used to set a lower bound on the amount of "nontreeness" in the data set when the true phylogeny is uncertain, as in Malinsky et al. (2018). Finally, there is also an option for the user to supply a tree in Newick format specifying known or hypothesized relationships between the populations or species. An output file with the "tree.txt" suffix then contains D and f_4-ratio values for trios ordered in a way consistent with this tree. This has to be done if the user later wants to calculate the f-branch statistic, because the statistic relies on a particular tree hypothesis. In all three types of

output, we order P1 and P2 so that $nABBA >= nBABA$. As a result, the D statistic is always positive and all the results, including the f_4-ratio and other statistics reflect evidence of excess allele sharing between P3 and P2 for each trio.

To assess whether D is significantly different from zero, `Dtrios` uses a standard block-jackknife procedure as in Green et al. (2010) and Durand et al. (2011), obtaining an approximately normally distributed standard error. For all three types of output, `Dtrios` calculates the Z-scores as $Z = D/std\_err(D)$, and outputs the associated p-values. However, when testing more than one trio, users should take into account the multiple testing problem and adjust the p-values accordingly. Although the different D statistics calculated on the same data set are not independent, a straightforward conservative approach is to consider them as such and to control for overall false discovery rate.

2.4.2 | The Dinvestigate program

The program `Dinvestigate` can provide further information about trios for which the D statistic is significantly different from zero by assessing whether the admixture signal is confined to specific loci and to assist in locating any such loci. For each trio specified by the user, the program outputs overall f_d, and f_{dM}, and also produces a text file which contains the values of f_d, f_{dM}, and df in sliding windows.

The size of the windows is specified by the user and refers to a fixed number of "informative" SNPs, i.e., SNPs that change the numerator of these statistics for any particular trio. We prefer this approach rather than specifying windows of fixed physical size (e.g., in kb), because equally sized physical windows can have vastly different amounts of information and the overall pattern of the results then tends to be driven by statistical noise – windows with fewer informative SNPs have more variance for all the calculated statistics.

2.4.3 | The Fbranch program

Given the "tree.txt" output of `Dtrios` or `DtriosCombine` and the same Newick format tree specifying known or hypothesized relationships between the populations or species, the `Fbranch` program outputs a matrix with f-branch statistic values for each branch on the tree, including internal branches, reflecting excess allele sharing with each valid population or species P3. The f-branch statistic results can be visualised by plotting this matrix using the `dtools.py` script, which we provide with the package. When calculating the f-branch statistic, it makes sense to set f_4-ratio results which are not statistically significant to zero, because f_4-ratio calculations for trios of nearly-equally closely related populations or species can produce large but nonsignificant values even in the absence of gene flow. Per default, our implementation sets all f_4-ratio values to zero where the p-value of the associated D statistic for that trio is > 0.01. This threshold can be changed by the user.

2.4.4 | The DtriosCombine utility

It is common practice, especially for larger data sets, that VCF files are divided into smaller subsets by genomic regions, e.g., per chromosome. This facilitates the parallelization of computational workflows. The `DtriosCombine` program enables parallel computation of the D and f_4-ratio statistics across genomic regions, by combining the outputs of multiple `Dtrios` runs, summing up the counts in Equation (4a–c) and the denominator of the f_4-ratio. It also calculates overall block-jackknife standard error across all regions to produce overall combined p-values for the D statistic.

2.4.5 | The DtriosParallel utility

We provide a convenient wrapper script for parallel `Dtrios` computation on a single computer or a compute node. The script optimally divides the `Dtrios` runs across the VCF file into a number of chunks which correspond to the number of available compute cores supplied by the used with the `--cores` option. The script waits for all the runs to complete and then automatically executes `DtriosCombine` to generate a single set of output files for the entire VCF data set.

3 | RESULTS AND DISCUSSION

We assessed the performance of `Dsuite` using three data sets (Malinsky et al., 2020): (a) variants mapping to the largest *Metriaclima zebra* reference genome scaffold (~16 Mb) from the data set of 73 species of Lake Malawi cichlid fishes published in Malinsky et al. (2018); (b) a small simulation data set comprising 20 species and 20 Mb of sequence generated using the `msprime` (Kelleher et al., 2016) software; (c) a large simulation data set with 100 Mb of sequence and 100 species. To confirm the validity of `Dsuite` results, D statistics and associated p-values from analysis of the Malawi cichlid data set were compared against the output of admixtools. The D values were found to be > 99.99% correlated between the two programs, and the p-values showed > 99% correlation. The results are thus qualitatively the same – the small differences in D include rounding errors, and for the p-values, the slightly larger differences are expected because of the stochasticity of the jackknife standard error estimation with different block sizes. In the simulated data, directional admixture events were simulated at randomly selected time points, with uniform distribution between the initial split time and the present, between a randomly selected pair of branches coexisting at that time point, and with admixture proportions drawn from a beta distribution rescaled to be between 0% and 30% with a maximum density around 5% to 10%. Diploid samples were produced by combining two independently simulated haploid sequences. Further details on the data sets and parameters used in the simulations are outlined in Table 2 and in the Appendix S1 document online.

TABLE 2 An outline of data sets used to evaluate the performance of `Dsuite`

						Simulation parameters			
Data set	Species	Samples	Trios	Sequence length	SNPs	μ, ρ^a (10^{-8})	N_e (10^3)	Gene flowevents	Age (generations)
Malawi scaffold_0	73	131	62,196	16 Mb	612,889	Empirical data			
Simulation small	20	40	1,140	20 Mb	4,342,771	1	50	5	1 million
Simulation large	100	200	161,700	100 Mb	97,201,601	1	50	10	1 million

[a]μ, per generation mutation rate; ρ, per-generation recombination rate

TABLE 3 A comparison of `Dsuite` and a number of other tools in terms of computational efficiency of *D* statistic estimation

Data set	Software	Options	Peak memory	Run time
Malawi scaffold_0	Dsuite `Dtrios`	--no-f4-ratio	92 MB	74 min 59 s
	Admixtools `qpDstat`	blgsize: 0.01	27,212 MB	125 min 2 s
	HyDe `run _ hyde.py`	none	178 MB	231 min 38 s
	Comp-D[a]	-d -H -b10	8,300 MB	24 hr+
	PopGenome	do.*df* = F block.size = 1,000	1,170 MB	24 hr+
Simulation small (20 species)	Dsuite `Dtrios`	--no-f4-ratio	8 MB	28 min 18 s
	Admixtools `qpDstat`	blgsize: 0.01	17,100 MB	13 min 59 s
	HyDe `run _ hyde.py`	none	258 MB	19 min 38 s
	Comp-D[a]	-d -H -b10	22,100 MB	24 hr+
	PopGenome	do.*df* = F block.size = 1,000	440 MB	1 min 50 s
Simulation large (100 species)	Dsuite `Dtrios`	--no-f4-ratio	223 MB	215 min 52 s (×100[b])
	Admixtools `qpDstat`	blgsize: 0.05	1,117,314 MB	331 min 39 s (×100[b])
	HyDe `run _ hyde.py`	none	18,716 MB	576 min 32 s (×100[b])
	Comp-D[a]	-d -H -b10	1,000,185 MB+	24 hr+ (×100[b])
	PopGenome	do.*df* = F block.size = 1,000	470 MB	274 min 53 s (×100[b])

[a]Comp-D cannot use allele frequencies calculated across multiple individuals, so only one individual per species included.

[b]Because of the size of the data set, we divided the analysis into 100 equally sized jobs to run in parallel; the run time and memory requirements are given for the first job.

3.1 | Computational efficiency

To assess computational efficiency of `Dsuite`, we calculated *D* statistics for all combinations of trios with four other software packages: admixtools, hyde, comp-d, and popgenome. ANGSD was not included in the comparisons because, unlike all the other programs, it uses read alignments instead of genotypes as the starting point for the analyses. For the Malawi cichlids and for the large simulated data sets, `Dsuite` was by far the most efficient of the programs in terms of both memory requirements and run time. For the small simulated data set, `Dsuite` was still the most memory efficient, but ADMIXTOOLS, HyDe, and especially PopGenome were faster. PopGenome also performed well on the large simulated data set – although slightly slower than `Dsuite`, it was the only other program competitive in both run time and memory requirements. The remaining programs required a lot of memory for the analysis of the large simulated data set – ADMIXTOOLS and Comp-D required >1 Terabyte of RAM and HyDe >18 Gigabytes, while the `Dsuite` run required ~223 MB. The difference in memory efficiency between `Dsuite` and especially ADMIXTOOLS and Comp-D remained more

than two orders of magnitude also for the two other data sets. In terms of speed, Comp-D stood out as being the slowest across all analyses. We cancelled all the Comp-D runs after 24 hr with only a small proportion of the trios completed. Among `Dsuite`, ADMIXTOOLS, and HyDe the run time differences were up to ~2–3 fold depending on the data set. The full results are shown in Table 3. We suggest that in addition to facilitating analyses of large data sets, improvements in computational efficiency may also facilitate the future inclusion of *D* and f_4-ratio as summary statistics within Approximate Bayesian Computation (ABC) inference frameworks (Beaumont et al., 2002; Jay et al., 2019).

While the `Dsuite` and PopGenome analyses were run directly on the VCF file, all other software required format conversion. For ADMIXTOOLS, we first obtained data in the PED format using VCFtools v0.1.12b (Danecek et al., 2011) with the `--plink` option, and then translated these into the software-specific EIGENSTRAT format using the `convertf` program, which is included in the ADMIXTOOLS package. Data conversion into the PHYLIP input format for HyDe and Comp-D was done using the vcf2phylip script (Ortiz, 2019). The additional run and set-up time needed for these conversions was excluded from the run times shown in Table 3.
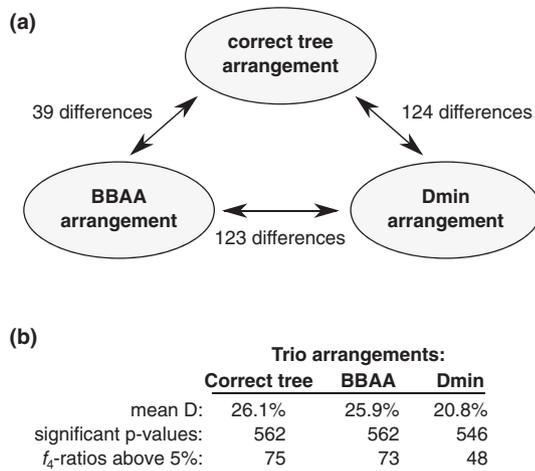
(a)

(b)

	Trio arrangements:		
	Correct tree	**BBAA**	**Dmin**
mean D:	26.1%	25.9%	20.8%
significant p-values:	562	562	546
f_4-ratios above 5%:	75	73	48

FIGURE 2 Summary of `Dtrios` output for the small simulated data set (20 species, 1,140 trios, five gene flow events). (a) The number of differences in trio arrangements between the three different output files. (b) A brief summary comparing the results with the three alternative arrangements

3.2 | Example and interpretation

In this section we use the small simulated data set to illustrate the outputs of `Dsuite` and some topics related to the interpretation of the results. The results for the Malawi cichlid data set are discussed in Malinsky et al. (2018).

We found tens of differences among the trio arrangements in the three output files produced by `Dsuite Dtrios` (Figure 2a). The "BBAA" trio arrangements differed from the correct tree in 39 cases (3.4% of the trios), which illustrates that sister species do not always share the most derived alleles in the presence of gene flow, even in the absence of rate variation. However, unlike for the simulation, the correct tree is not known for most real-world data sets and the frequency of the "BBAA" pattern may then be a useful guide regarding the population relationships. The "Dmin" arrangements differed from the correct tree in 124 trios (10.9%).

Keeping in mind that only five gene flow events were simulated, it is notable that almost half of the D statistics were significantly elevated, e.g., 546 (47.9%) even in the "Dmin" arrangement which provides a lower bound on the D value for each trio (Figure 2b). Using the f_4-ratio measure, we found that admixture proportions above 5% were estimated for at least 48 trios. This demonstrates that D and f_4-ratio statistics are correlated and that a significantly elevated result for a trio does not necessarily pinpoint the populations involved in a gene flow event.

The tree in Figure 3 shows the true simulated relationships between the 20 species together with the five gene flow events and their admixture proportions. The output of `Dsuite Fbranch` inference is then plotted in the inset heatmap, revealing how the f-branch statistic is useful in guiding the interpretation of correlated f_4-ratio results. Ten out of the 568 f-branch (f_b) signals are stronger than 5%, much fewer than the 73 signals identified from the raw trio analysis with the "BBAA" trio arrangements.

FIGURE 3 Results of `Fbranch` for the small simulated data set. The true species tree, which was used as input for simulating the data, is shown along the sides. The red arrows correspond to the simulated gene flow events and true admixture proportions. The tree is displayed in an 'expanded' form along the y axis, so that each branch, including internal branches, points to a corresponding row in the matrix with inferred f-branch statistics. The values in the matrix thus refer to excess allele sharing between the branch b identified on the expanded tree on the y axis (relative to its sister branch) and the species P3 identified on the x-axis. As an example, the cell highlighted by the black arrow refers to excess allele sharing between species g and the branch leading to species m, relative to its sister, the internal branch above species n, o, p, and q [Colour figure can be viewed at wileyonlinelibrary.com]
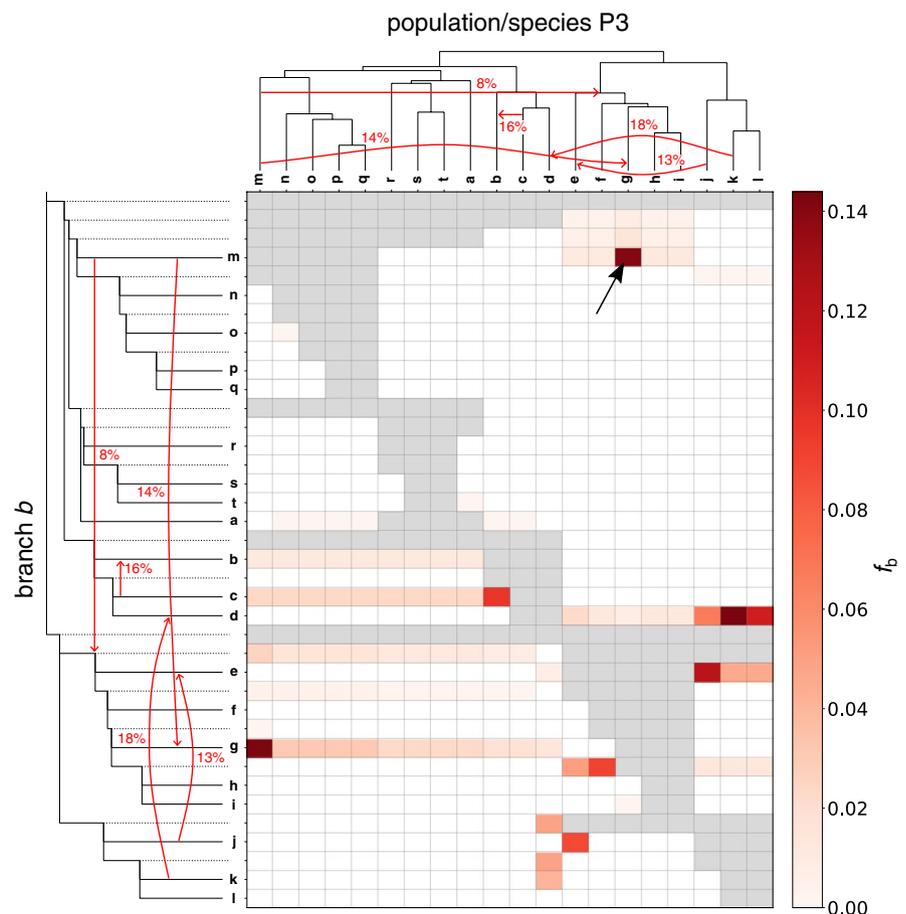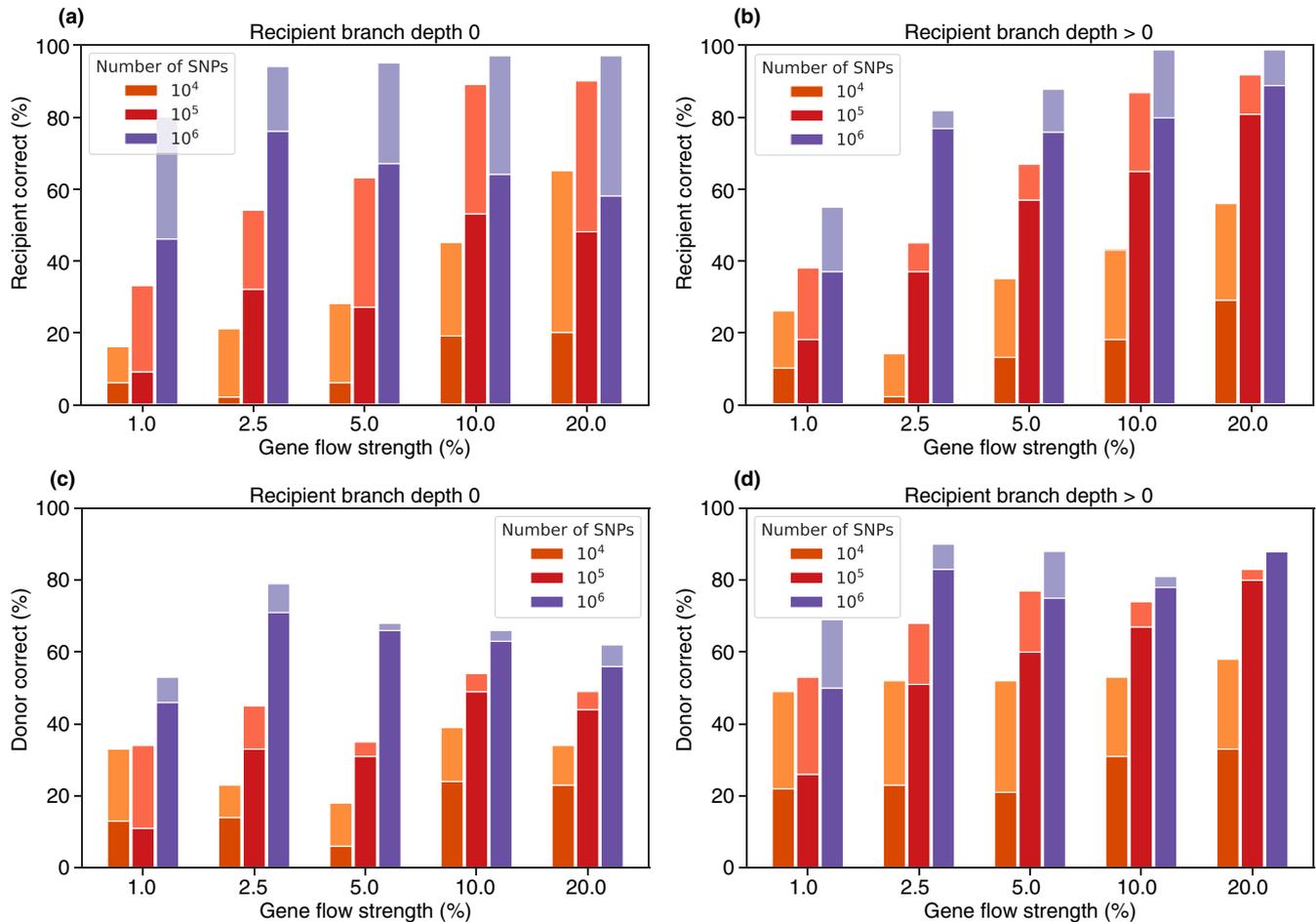
FIGURE 4 Simulation based assessment of *f*-branch accuracy. The barplots show the proportion of cases where the strongest inferred *f*-branch signal corresponds the correct simulated gene flow recipient and donor branches. We simulated a single gene flow event randomly placed on a 20-species tree. The lighter shaded areas of each bar correspond to cases where, rather than the actual recipient/donor branches, their sister branches showed the strongest signal. (a–b) Proportion of times that the branch *b* of the strongest *f*-branch signal corresponds to the true recipient of gene flow in cases where the recipient branch is (a) a terminal or (b) an internal branch. (c–d) Proportion of times that P3 of the strongest *f*-branch signal corresponds to the true donor of gene flow or to a descendant branch of it for cases where the recipient branch is (c) a terminal or (d) an internal branch [Colour figure can be viewed at wileyonlinelibrary.com]

The reduction of information and the visualization provided by *f*-branch facilitates narrowing down the number of possible acceptor and donor lineages involved in a gene flow event and should be seen as an aid for formulating specific gene flow hypotheses in a large data set that can be followed up individually by other methods, for example in a more richly parametrised model-based inference framework by software such as FASTSIMCOAL2 (Excoffier et al., 2013) or δaδi (Gutenkunst et al., 2009). In particular, the 10 *f*-branch signals stronger than 5% correctly identify seven out of the nine branches involved in gene flow events. Six of these signals correctly pinpoint both branches involved in gene flow events ([d, k], [e, j], [m, g], [c, b]). However, a single gene flow event between two branches can still produce more than one *f*-branch signal. For example, the gene flow event from m into g above produces elevated values for both $f_{b=g}(P3 = m)$, i.e., the branch leading to g and species m, and its "mirror image" $f_{b=m}(P3 = g)$, branch leading to m and species g. While such mirror images are a common feature of the *f*-branch, we note

that the statistic is not designed to be symmetric, because the f_4-ratios themselves, and the trees on which the statistics are based, are not symmetric with respect to switching P2 and P3. Furthermore, the gene flow from m into g produces correlated signals between g and lineages related to m (e.g., n, o, p, q) because of the shared ancestry between these lineages and m. This generally manifests in horizontal lines of correlated signals in the *f*-branch plots as shown in Figure 3. Finally, note that an *f*-branch result in itself does not indicate directionality of gene flow. We suggest using 5-taxon tests, when possible, for inferring directionality (Pease & Hahn, 2015; Svardal et al., 2020).

3.3 | Assessment of *f*-branch accuracy

Malinsky et al. (2018) first introduced the *f*-branch statistic and tested its behaviour on a simple simulated data set of eight species,

comparing its behaviour against inference with the TREEMIX software (Patterson et al., 2012; Pickrell & Pritchard, 2012). They found the *f*-branch statistic to be more robust in detecting branches involved in hybridisation events in cases where gene flow was particularly strong. Here, we provide an additional assessment of *f*-branch inference accuracy on a simulated data set of 20 species, reflecting the focus on Dsuite and the overall trend towards analyses of larger data sets.

We examine how often the strongest inferred *f*-branch signal corresponds to the correct gene flow donor and recipient branches within the species tree in a scenario with one gene flow event, depending on gene flow strength and the number of SNPs used as input for the inference. For this, we selected numbers whose magnitude approximates common sequencing strategies: 10^4 SNPs corresponding to RADseq experiments, 10^5 SNPs corresponding to transcriptome sequencing or exome capture studies, and 10^6 SNPs which corresponds in magnitude to the size of data sets obtained by whole genome (re-)sequencing experiments. The results are shown in Figure 4. See Appendix S1 for more details about how these simulations and inference were performed.

With 10^6 SNPs, *f*-branch inference was accurate in the majority of cases for both donor and recipient branches where the simulated gene flow was stronger than 2.5%. Inference for gene flow on internal branches, which is a key benefit of the *f*-branch statistic, was more accurate than for terminal branches (compare Figure 4a, c against Figure 4b, d). We note that performance depends on the number of SNPs used. The inferences corresponding to RAD-seq were accurate in only < 40% of the simulations, even when the simulated gene flow strength was substantial. Therefore, while RAD-seq data can be used successfully to estimate *D* statistics and the f_4-ratio, the simulations suggest that *f*-branch results should be treated with caution for this data type. The inferences corresponding to transcriptome or exome capture data performed better and inferred internal donor and recipient branches correctly in the majority of the cases, as long as the simulated gene-flow was > 1%. A further improvement is seen with whole genome data, where *f*-branch can deliver good accuracy for both internal and external branches in 20-species trees, as long as gene flow proportions are over 1%.

4 | CONCLUSIONS

The Dsuite software package brings together a number of statistics to learn about admixture history from patterns of allele sharing across populations or closely related species. In particular, by being computationally efficient, it facilitates the calculation of the *D* and f_4-ratio statistics across tens or even hundreds of populations, meeting the needs of ever-growing genomic data sets. Correct interpretation of the results of a system of *D* and f_4-ratio tests remains challenging and is an active area of research. In real data sets, imbalances in allele sharing that lead to significantly elevated *D* and f_4-ratio statistics can result from specific scenarios involving ancestral population structure (Durand et al., 2011; Eriksson & Manica, 2012) and variation in substitution rates (Pease

& Hahn, 2015). Even when all allele sharing imbalances are caused by introgression, more work remains to be done to reliably pinpoint all introgression events and infer the networks of gene flow that may characterise relationships between many populations or closely related species. Dsuite implements tools that aid the interpretation of the results, including the f_d, f_{dM}, and d_f statistics suited for applying to genomic windows and the *f*-branch statistic which aids in assigning the gene flow to particular branches on the population or species tree.

CONFLICT OF INTEREST
None declared.

AUTHOR CONTRIBUTIONS
MilMal developed the Dsuite software package with assistance from MicMat regarding tree-based operations. H.S. conceived the *f*-branch statistics, coded the plotting function for it, and performed the simulations. H.S. also wrote the DtriosParallel script. MilMal wrote the manuscript with contributions from H.S. and MicMat. All authors approved the manuscript.

DATA AVAILABILITY STATEMENT
The Malawi cichlid data and the simulated data used in this manuscript are available through the Dsuite GitHub repository (https://github.com/millanek/Dsuite). They are also archived, together with a snapshot of the Dsuite code, on DataDryad under https://doi.org/10.5061/dryad.tdz08kpxt (Malinsky et al., 2020).

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SUPPORTING INFORMATION

Additional supporting information may be found online in the Supporting Information section.